DS-GA.3001 Embodied Learning and Vision

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NYU

Spring 2025

embodied-learning-vision-course.github.io



### Lecture Slides for Note Taking





Module 5: Continual Learning, Few-Shot Learning, Meta-Learning



## Why Continual Learning?

• The world is not a dataset that allows you to get IID samples.



# Why Continual Learning?

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- The world keeps changing and evolving.



# Why Continual Learning?

- The world is not a dataset that allows you to get IID samples.
- The world keeps changing and evolving.
- Online vs. Continual
  - Online means that samples arrive in a streaming / temporal partial order, but they may still come from a static distribution.

$$\theta_t = f(x_t, \theta_{t-1}) \quad x_{1:T} \sim \mathcal{X}$$

- Example: Online reinforcement learning, trajectory roll out is online, but the environment is the same.
- Continual learning means that there will be distribution shift.



- Distribution shift: Forgetting
  - Learning on A and then B, results in worse performance on A.



- Distribution shift: Forgetting
  - Learning on A and then B, results in worse performance on A.
- Multi-task learning: Forward transfer
  - Learning Task A + B results in better learning in Task C compared to learning C alone.
  - Leverage the similarity between tasks.



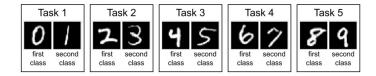
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- Compositionality
  - Learning A and B first, and then learning tasks with composed A+B.

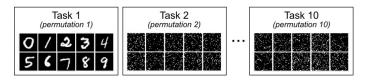


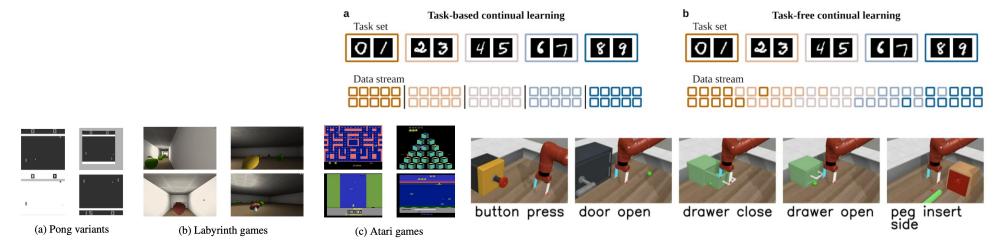
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- Compositionality
  - Learning A and B first, and then learning tasks with composed A+B.
- Incremental/curriculum Learning
  - Learning A->B->C is easier than at random order.



• Learning a sequence of tasks without looking back.







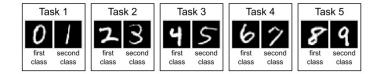
- Learning a sequence of tasks without looking back.
- Goal is to do well on all of the tasks at the end.

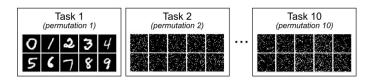
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Task set

Data stream

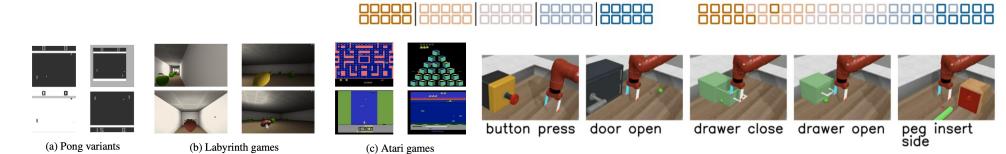
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Data stream





Task-based continual learning

67

89

2345



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Task set

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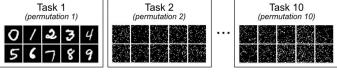
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• Task boundary



Task 2

Task 1



Task 3

Task 4

Task 5

class





Data stream



Task-based continual learning

45

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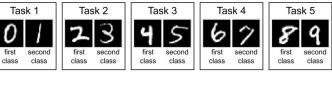
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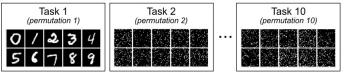


Task-based continual learning

- Learning a sequence of tasks without looking back.
- Goal is to do well on all of the tasks at the end.
- Task boundary
- Memory constraints

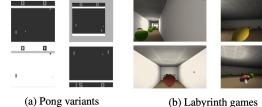










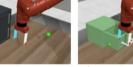




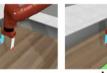


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(c) Atari games

button press door open drawer close drawer open

peg insert side



#### Parameter Regularization

• Over-completeness Assumption. A multitude of models can reach equivalent performance.

 $S_A = \{ \theta \mid \ell_A(\theta) < \epsilon \}$  $S_A \cap S_B \neq \emptyset$ 

#### Parameter Regularization

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- What is left is to efficiently find the intersection between A and B.

 $p(\theta \mid \mathcal{D}_A) = \mathcal{N}(\theta; \theta^*, \Sigma)$ 

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### Parameter Regularization

- Over-completeness Assumption. A multitude of models can reach equivalent performance.
- What is left is to efficiently find the intersection between A and B.

 $p(\theta \mid \mathcal{D}_A) = \mathcal{N}(\theta; \theta^*, \Sigma)$ 

• Elastic Weight Consolidation (EWC):

$$\mathcal{L}(\theta) = \mathcal{L}_B(\theta) + \sum_i \frac{\lambda}{2} F_i (\theta_i - \theta_{A,i}^*)^2$$

$$S_A \cap S_B \neq \emptyset$$

$$\square \text{ Low error for task B} = EWC$$

$$\square \text{ Low error for task A} = L_2$$

$$\square \text{ no penalty}$$

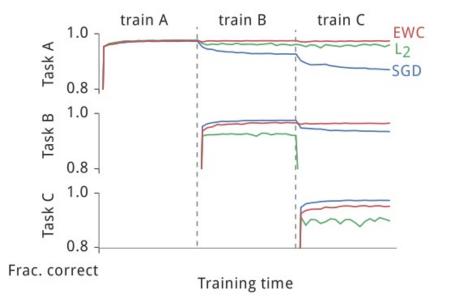
 $\mathcal{S}_A = \{\theta \mid \ell_A(\theta) < \epsilon\}$ 



## **Computing Fisher**

• At the end of each epoch, compute the gradient squared:  $(12)^2$ 

$$F_i = \left(\frac{d\mathcal{L}}{d\theta_i}\right)$$



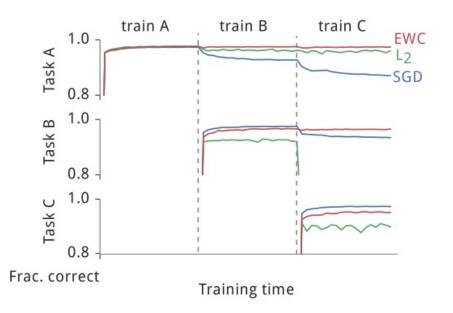


## Computing Fisher

• At the end of each epoch, compute the gradient squared:

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• Measures the sensitivity on each parameter dimension.



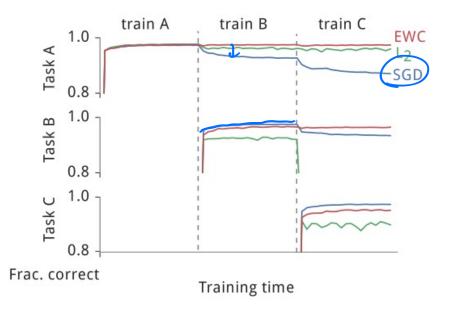


# **Computing Fisher**

• At the end of each epoch, compute the gradient squared:

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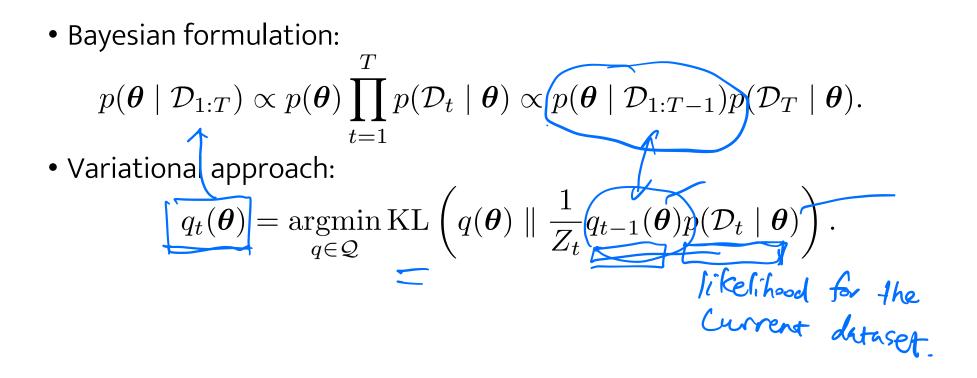
- Measures the sensitivity on each parameter dimension.
- You can also accumulate an online estimate.





• Bayesian formulation:  $\mathcal{D}_{1:T}) \propto p(\boldsymbol{\theta}) \prod p(\mathcal{D}_t \mid \boldsymbol{\theta}) \propto p(\boldsymbol{\theta} \mid \mathcal{D}_{1:T-1}) p(\boldsymbol{\theta})$  $\boldsymbol{\theta}$ t=1







• Bayesian formulation:

$$p(\boldsymbol{\theta} \mid \mathcal{D}_{1:T}) \propto p(\boldsymbol{\theta}) \prod_{t=1}^{T} p(\mathcal{D}_t \mid \boldsymbol{\theta}) \propto p(\boldsymbol{\theta} \mid \mathcal{D}_{1:T-1}) p(\mathcal{D}_T \mid \boldsymbol{\theta}).$$

• Variational approach:

$$q_t(\boldsymbol{\theta}) = \underset{q \in \mathcal{Q}}{\operatorname{argmin}} \operatorname{KL} \left( q(\boldsymbol{\theta}) \parallel \frac{1}{Z_t} q_{t-1}(\boldsymbol{\theta}) p(\mathcal{D}_t \mid \boldsymbol{\theta}) \right).$$
  
Loss:  $\mathcal{L}(q_t(\boldsymbol{\theta})) = \mathbb{E}_{\boldsymbol{\theta} \sim q_t(\boldsymbol{\theta})} [-\log p(\mathbf{y} \mid \mathbf{x}, \boldsymbol{\theta})] + \operatorname{KL}(q_t(\boldsymbol{\theta}) \parallel q_{t-1}(\boldsymbol{\theta})).$ 



•

• Bayesian formulation:

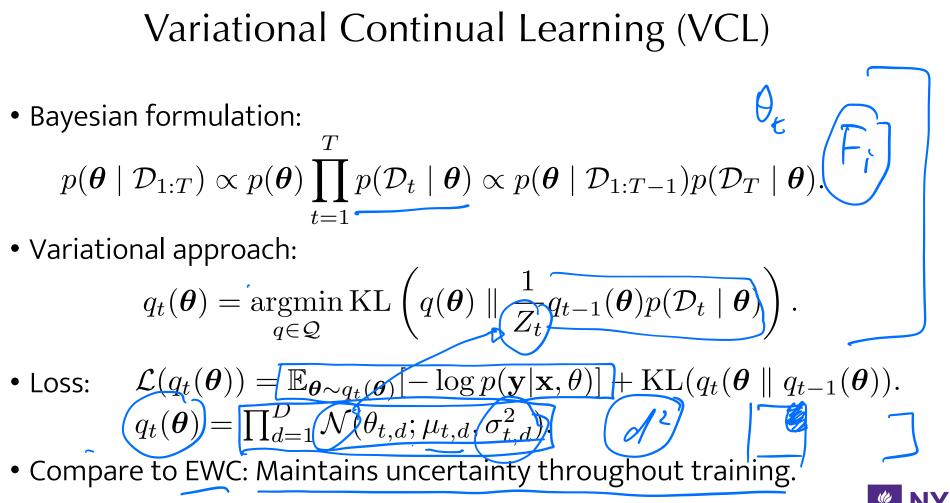
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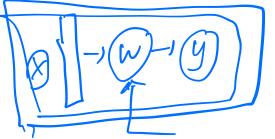
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• Loss:  $\mathcal{L}(q_t(\boldsymbol{\theta})) = \mathbb{E}_{\boldsymbol{\theta} \sim q_t(\boldsymbol{\theta})}[-\log p(\mathbf{y}|\mathbf{x}, \boldsymbol{\theta})] + \mathrm{KL}(q_t(\boldsymbol{\theta} \parallel q_{t-1}(\boldsymbol{\theta}))).$  $q_t(\boldsymbol{\theta}) = \prod_{d=1}^D \mathcal{N}(\theta_{t,d}; \mu_{t,d}, \sigma_{t,d}^2).$ 







EBM for Continual Learning

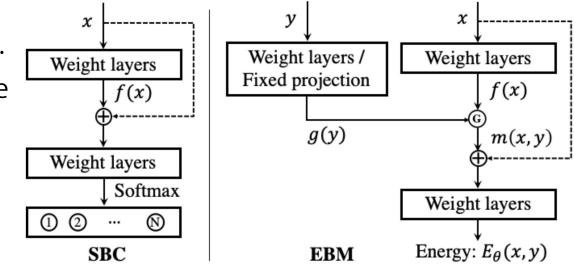


• Softmax layer is known to be y х х sensitive to distribution shift. Weight layers / Weight layers Weight layers X Fixed projection f(x)f(x)g(y)m(x,y)Weight layers Softmax Weight layers 2 N (1)••• Energy:  $E_{\theta}(x, y)$ SBC **EBM** 



### EBM for Continual Learning

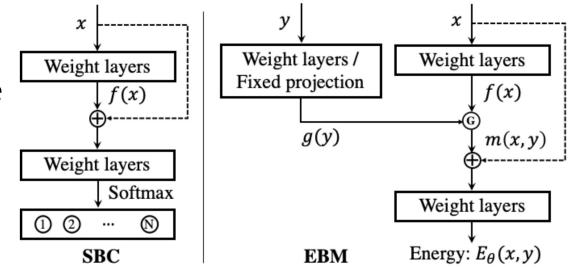
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- A common approach is to use nearest mean classifier.





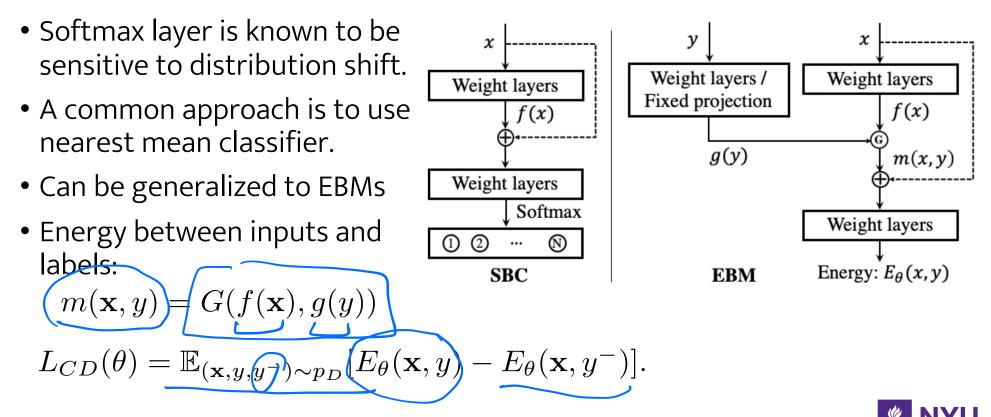
### EBM for Continual Learning

- Softmax layer is known to be sensitive to distribution shift.
- A common approach is to use nearest mean classifier.
- Can be generalized to EBMs



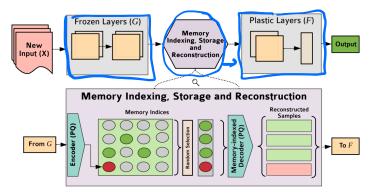


### EBM for Continual Learning

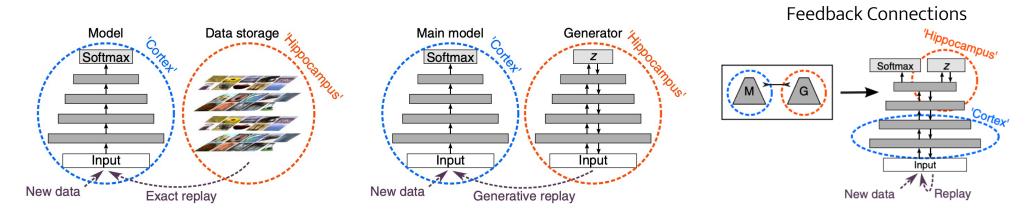


Li et al. Energy-Based Models for Continual Learning. CoLLAs 2022.

# Replay

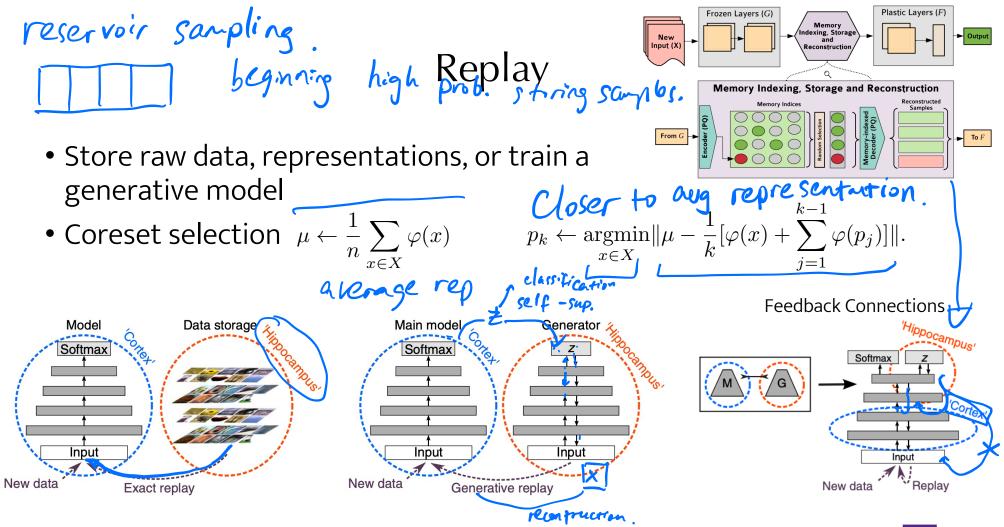


• Store raw data, representations, or train a generative model generative raplay.



Rebuffi et al. iCaRL: Incremental Classifier and Representation Learning. CVPR 2017. van de Ven et al. Brain-inspired replay for continual learning with artificial neural networks. Nature communications 2020. Hayes et al. REMIND Your Neural Network to Prevent Catastrophic Forgetting. ECCV 2020.

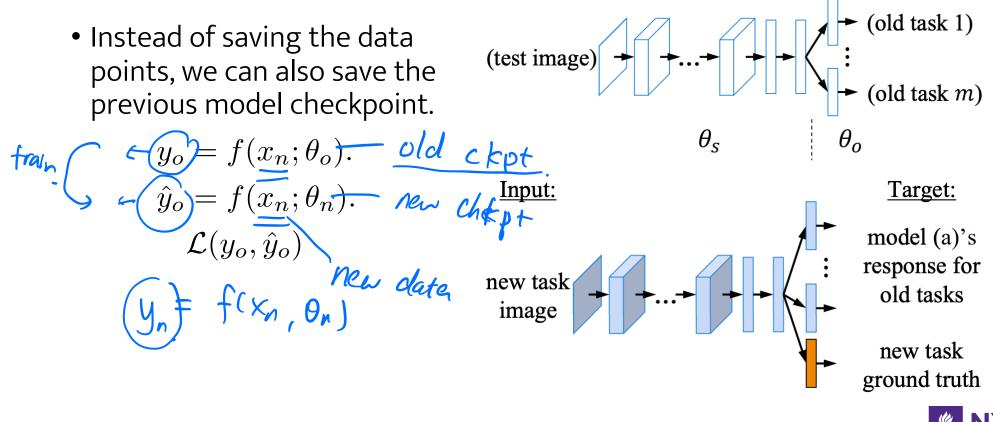




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### **Knowledge Distillation**

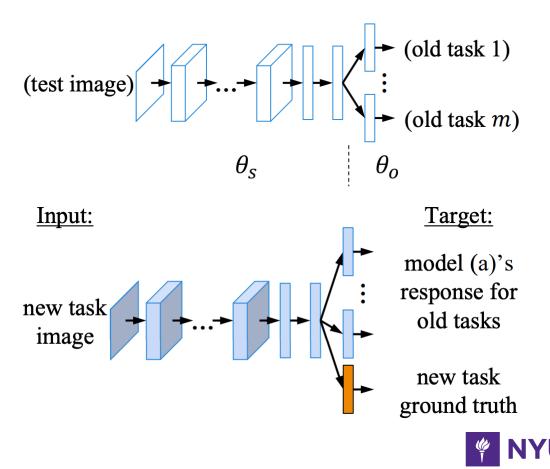


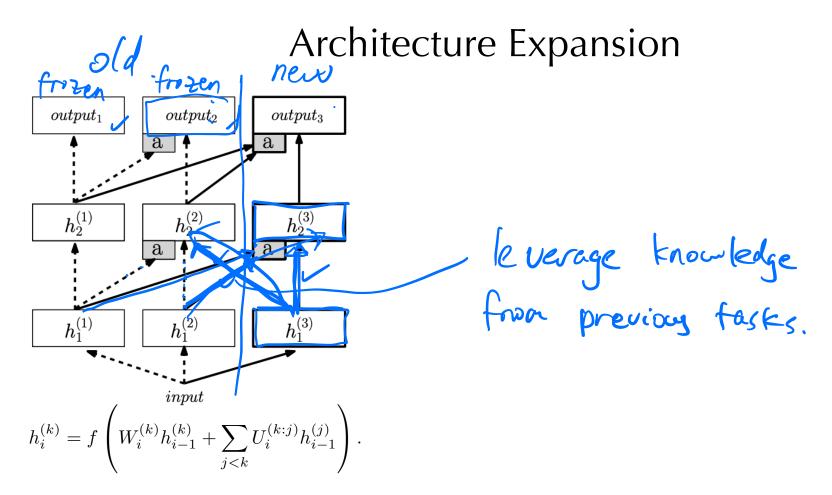
### Knowledge Distillation

• Instead of saving the data points, we can also save the previous model checkpoint.

$$y_o = f(x_n; \theta_o).$$
$$\hat{y}_o = f(x_n; \theta_n).$$
$$\mathcal{L}(y_o, \hat{y}_o)$$

 Use <u>new data points and old</u> weights to "distill"

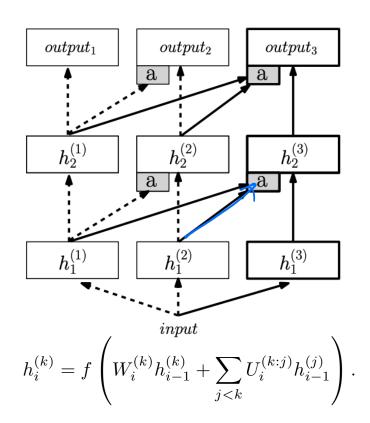




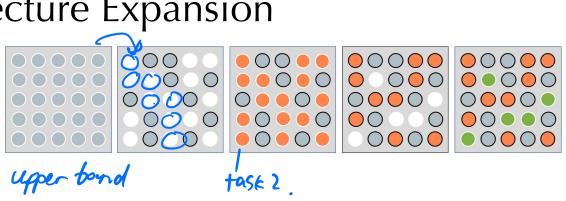
Rusu et al. Progressive Neural Networks. NIPS 2016 Deep Learning Symposium. PackNet: Adding Multiple Tasks to a Single Network by Iterative Pruning. CVPR 2018. Yoon et al. Lifelong Learning with Dynamically Expandable Networks. ICLR 2018.



#### Architecture Expansion

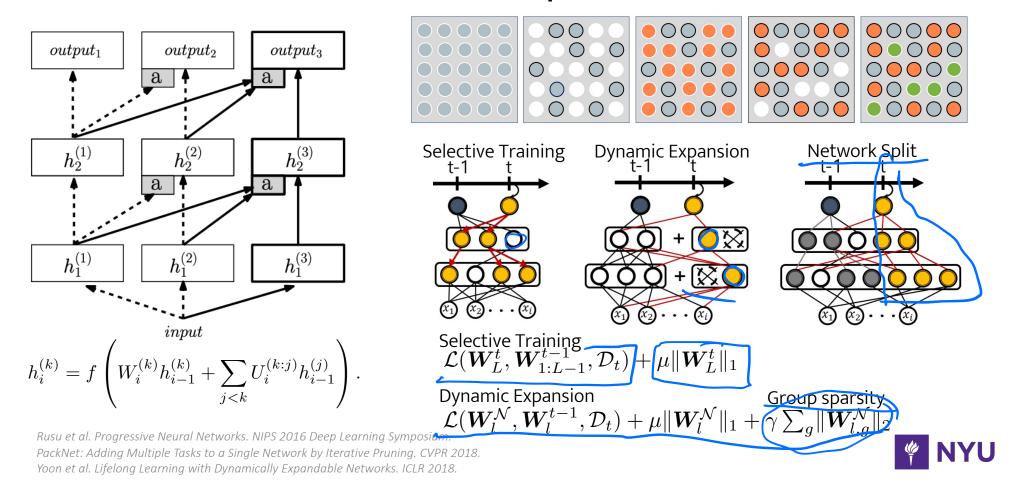


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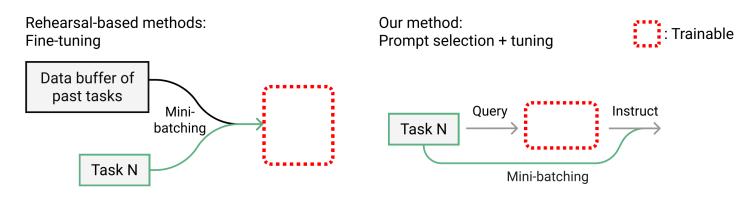


#### Architecture Expansion



# Adapting Pretrained Models

• Pretrained models have general knowledge that can be adapted to a continual stream of tasks.

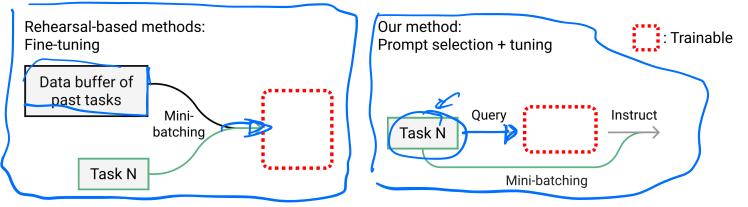




Wang et al. Learning to Prompt for Continual Learning. CVPR 2022.

# Adapting Pretrained Models

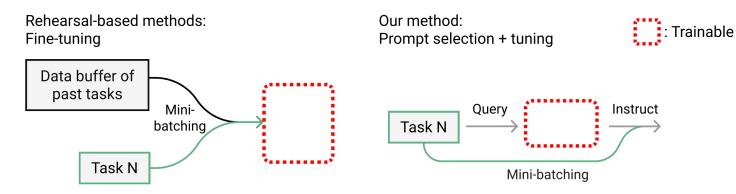
- Pretrained models have general knowledge that can be adapted to a continual stream of tasks.
- Learn adaptation parameters for each task and store these as "task embeddings."





# Adapting Pretrained Models

- Pretrained models have general knowledge that can be adapted to a continual stream of tasks.
- Learn adaptation parameters for each task and store these as "task embeddings."
- Main model is frozen.



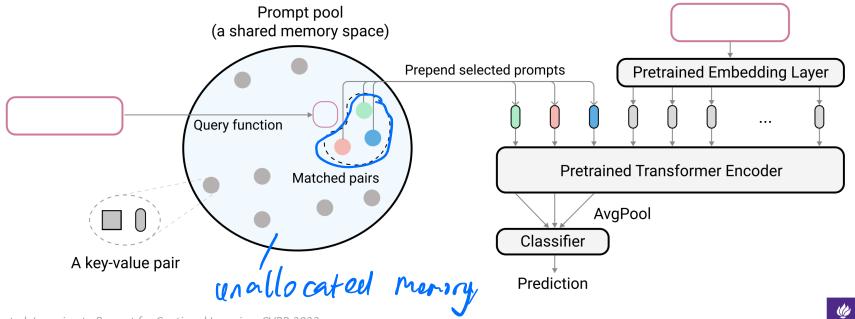


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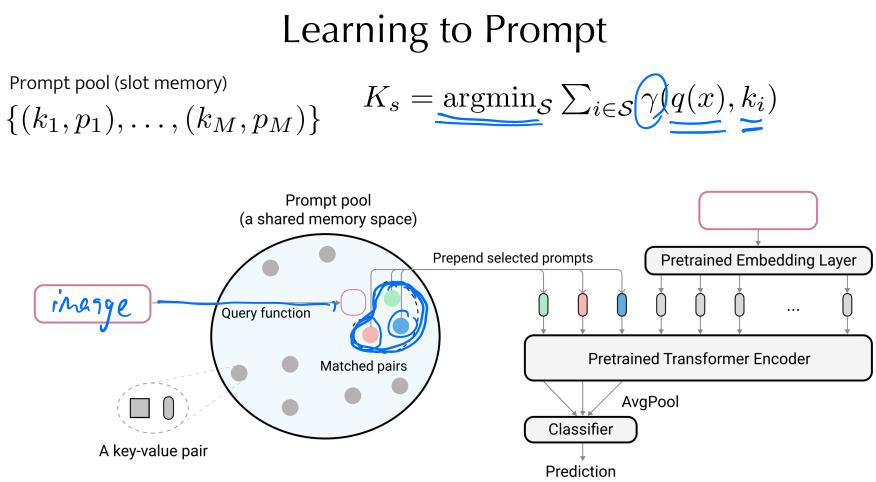
### Learning to Prompt

Prompt pool (slot memory)

 $\{(k_1, p_1), \ldots, (k_M, p_M)\}$ 

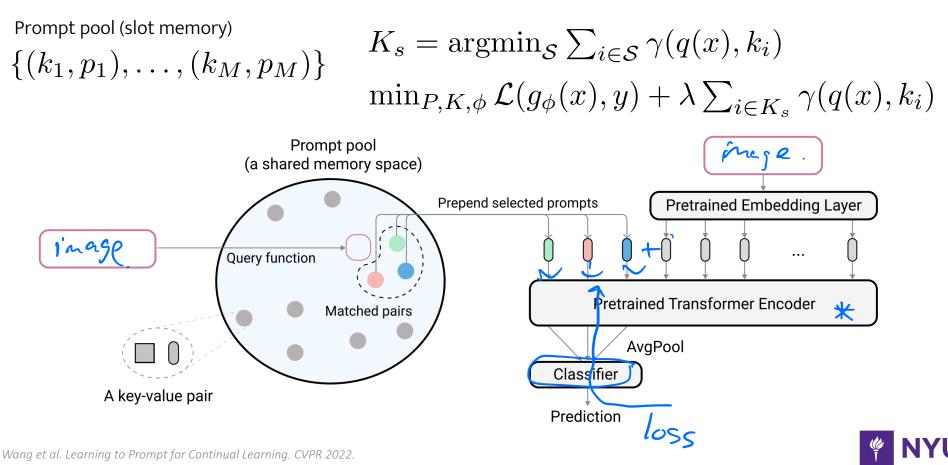


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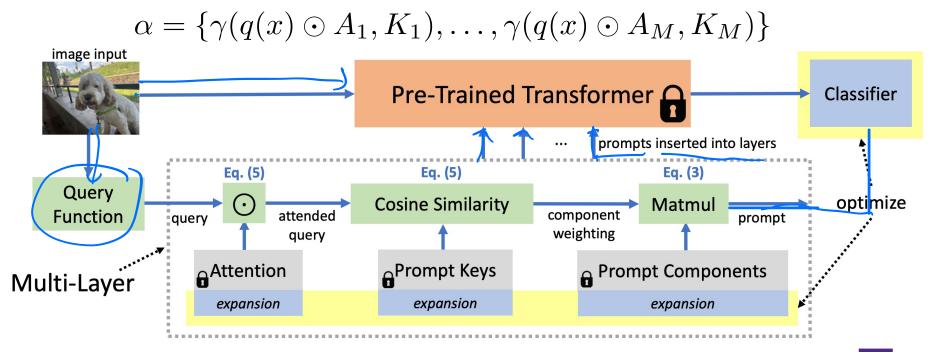


### Learning to Prompt



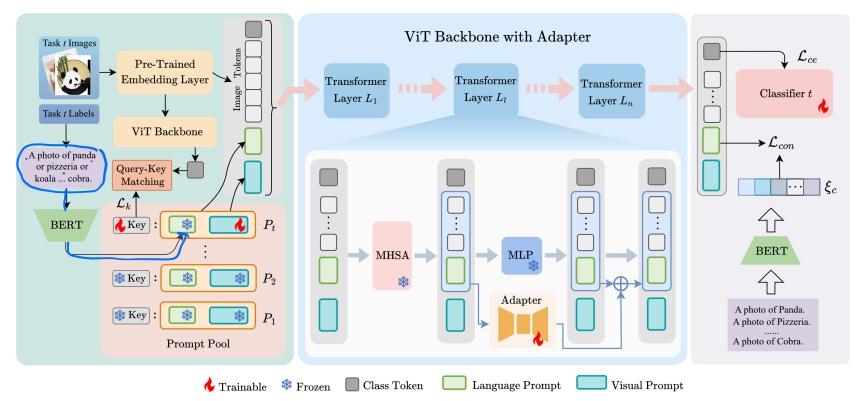
## Learned Prompt Query

• The query function can be end-to-end learned.



*Smith et al. CODA-Prompt: COntinual Decomposed Attention-based Prompting for Rehearsal-Free Continual Learning. CVPR 2023.* 

#### **Multimodal Semantic Prompts**





forgetting.

• Fragility of feedforward gradient descent of the entire networks



- Fragility of feedforward gradient descent of the entire networks
- If we have representations ready, continual learning is just memorizing a sequence of new tasks.



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- In prompting approaches:

prompt pool = memorypretrained network = representations

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- But what if representations also need to be built sequentially?



- Fragility of feedforward gradient descent of the entire networks
- If we have representations ready, continual learning is just memorizing a sequence of new tasks.
- In prompting approaches:
  - prompt pool = memory
  - pretrained network = representations
- But what if representations also need to be built sequentially?
- It's also plausible that representations are just "deeper memory."





• Memory aims to store content for easy retrieval







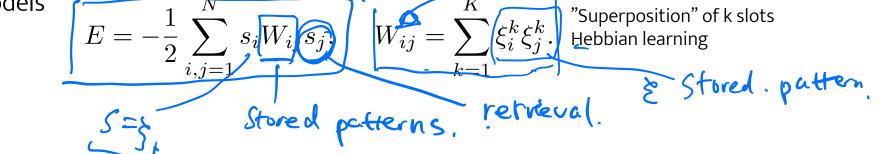
- Memory aims to store content for easy retrieval
  - Associative memories (Hopfield Networks) can be viewed as energy-based models



*Krotov & Hopfield. Dense Associative Memory for Pattern Recognition. NIPS 2016. https://ml-jku.github.io/hopfield-layers/* 



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- Memory aims to store content for easy retrieval
  - Associative memories (Hopfield Networks) can be viewed as energy-based models
     1 N
     1 N
     1 Superposition of k slots

$$E = -\frac{1}{2} \sum_{i,j=1} s_i W_{ij} s_j, \qquad W_{ij} = \sum_{k=1}^{k} \xi_i^k \xi_j^k.$$
 Hebbian learning

• When presented with a new pattern the network should respond with a stored memory which most closely resembles the input.

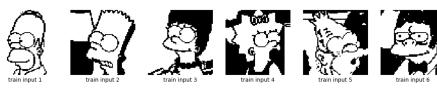




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     N
     K
     "Superposition" of k slot

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 "Superposition" of k slot

- When presented with a new pattern the network should respond with a stored memory which most closely resembles the input.
- Retrieval:  $s_i = (\text{sign}(\sum_j W_{ij}s_j))$





masked test image

Storage:  $C pprox_{c}$ 



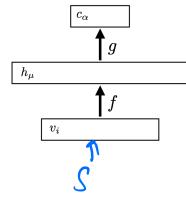


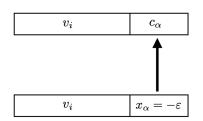
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Krotov & Hopfield. Dense Associative Memory for Pattern Recognition. NIPS 2016. https://ml-jku.github.io/hopfield-layers/

• Duality with a feedforward network.

$$E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i})$$



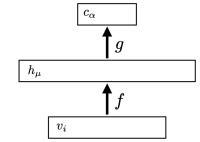


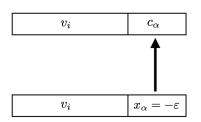


• Duality with a feedforward network.

 $E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i})$ 

• Non-linearity allows us to store more patterns.



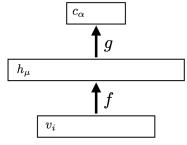


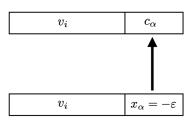


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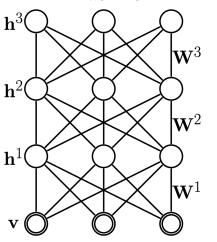
 $E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i})$ 

- Non-linearity allows us to store more patterns.
- Deep Boltzmann machines





Deep Boltzmann Machine



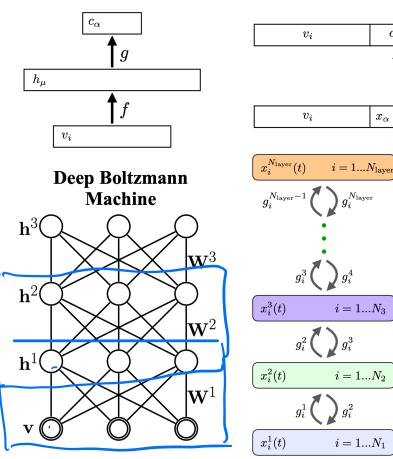
Salakhutdinov & Hinton. Deep Boltzmann Machines. AISTATS 2009. Krotov. Hierarchical Associative Memory. arXiv 2021.



• Duality with a feedforward network.

 $E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i})$ 

- Non-linearity allows us to store more patterns.
- Deep Boltzmann machines
- Hierarchical associative memory



 $c_{\alpha}$ 

 $x_{\alpha} = -\varepsilon$ 

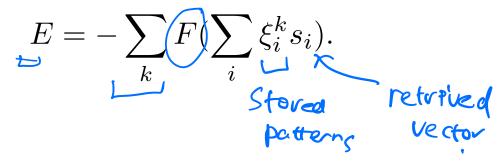
 $\xi_{ij}^{(N_{\mathrm{layer}},N_{\mathrm{layer}}-1)}$ 

 $\xi_{ii}^{(4,3)}$ 

 $\xi_{ij}^{(3,2)}$ 

 $\xi_{ii}^{(2,1)}$ 

Salakhutdinov & Hinton. Deep Boltzmann Machines. AISTATS 2009. Krotov. Hierarchical Associative Memory. arXiv 2021.

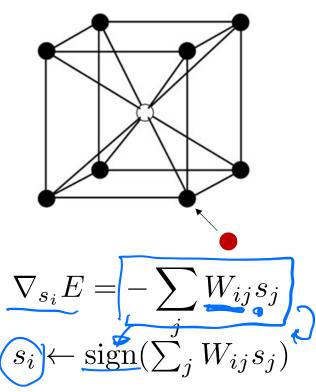




• General form:

$$E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i}).$$

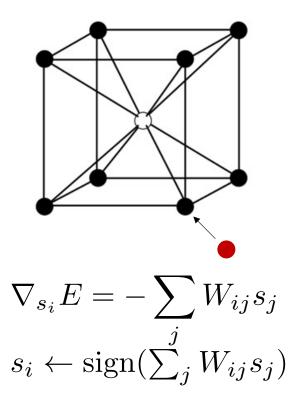
• When  $F(z) = z^2$  it gives the classic HN.





$$E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i}).$$

- When  $F(z) = z^2$  it gives the classic HN. Transformer-like attention operation:

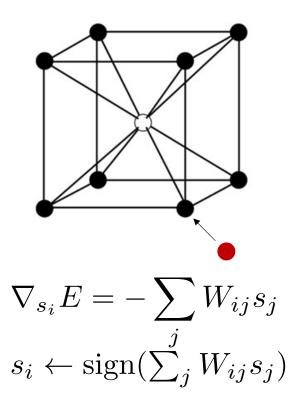




$$E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i}).$$

- When  $F(z) = z^2$  it gives the classic HN.
- Transformer-like attention operation:

$$\boldsymbol{Z} \leftarrow \operatorname{softmax}(\boldsymbol{\beta} \boldsymbol{X} \boldsymbol{W}_{\boldsymbol{q}} \boldsymbol{W}_{\boldsymbol{k}}^{\top} \boldsymbol{Y}^{\top}) \boldsymbol{Y}_{i} \boldsymbol{W}_{v}.$$

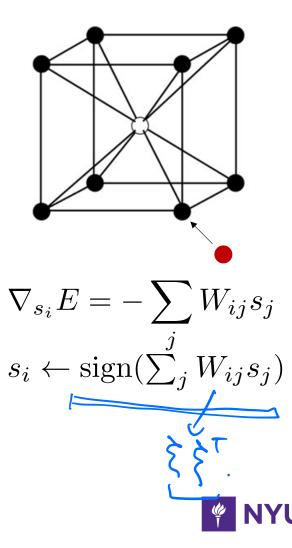




$$E = -\sum_{k} F(\sum_{i} \xi_{i}^{k} s_{i}).$$

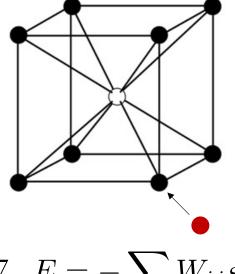
- When  $F(z) = z^2$  it gives the classic HN.
- Transformer-like attention operation:

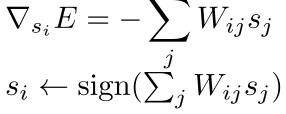
$$Z \leftarrow \operatorname{softmax}(\beta X W_q W_k^\top Y^\top) Y_i W_v.$$
$$S \leftarrow \operatorname{softmax}(\beta S \Xi^\top) \Xi. \rightarrow \nabla \Box$$



- General form:  $E = -\sum F(\sum \xi_i^k s_i).$ • Relation to Transformers
- When  $F(z) = z^2$  it gives the classic HN.
- Transformer-like attention operation:

$$Z \leftarrow \operatorname{softmax}(\beta X W_q W_k^\top Y^\top) Y_i W_v. \qquad s_i \leftarrow \operatorname{sign} S \leftarrow \operatorname{softmax}(\beta S \Xi^\top) \Xi. \quad l \quad \text{step}.$$
$$E = -\operatorname{logsumexp}(\beta, \Xi^\top s) + \frac{1}{2} s^\top s + \beta^{-1} \log N + \frac{1}{2} M^2$$

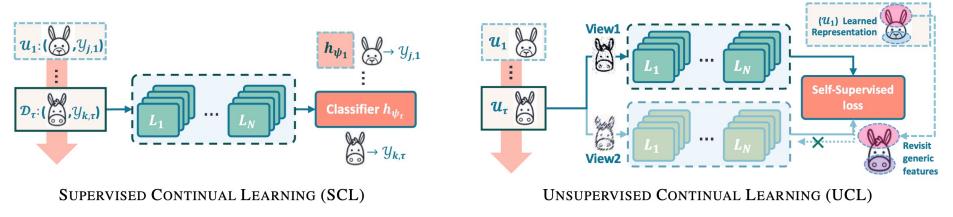






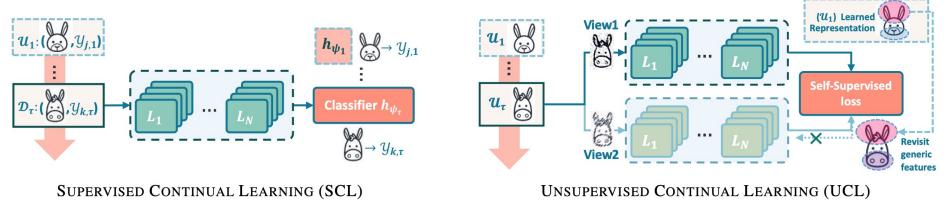
Ramsauer et al. Hopfield Networks is All You Need. ICLR 2021.

• Learning from a stream of unlabeled inputs.



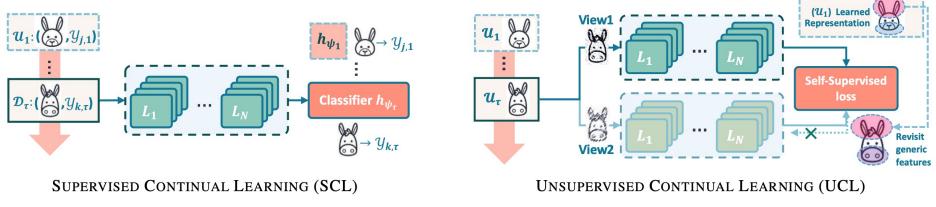


- Learning from a stream of unlabeled inputs.
- Bring SSL to the dynamic world.

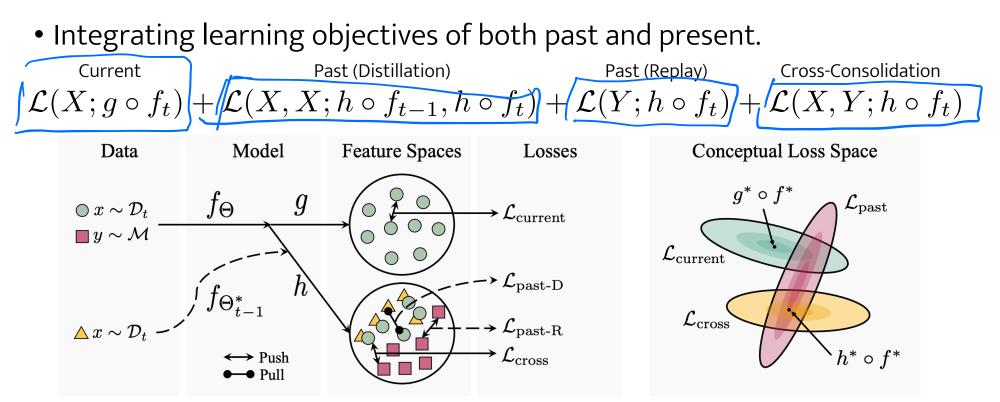




- Learning from a stream of unlabeled inputs.
- Bring SSL to the dynamic world.
- SSL can still suffer from distributional shifts.









## Outlooks

160M LLM 1B LLM Q 3 3 Loss on Task 1 T N Loss on Task 1 0 0 50 75 100 Training Episode Ó 25 25 50 75 1 Training Episode Ó 100

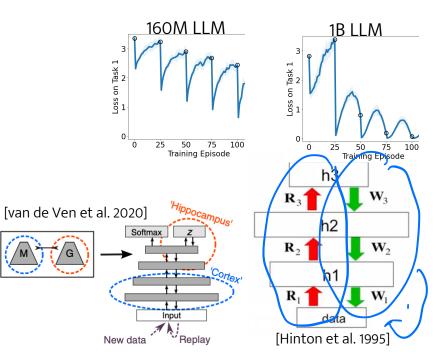
• Understand continual learning at scale

[Mayo et al. 2023]



# Outlooks

- Understand continual learning at scale
- Unified learning architecture, objective and replay, role of sleep

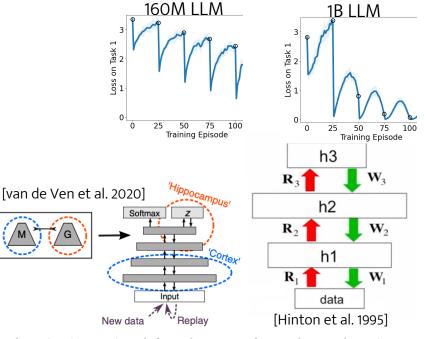


[Mayo et al. 2023]

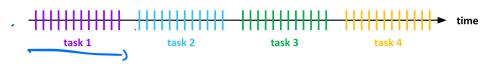


# Outlooks

- Understand continual learning at scale
- Unified learning architecture, objective and replay, role of sleep
- Continual learning with real world structure



Typical setting in continual, few-shot, transfer, and meta-learning



 Typical setting of human learning [Mayo et al. 2023]

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Tasks are interspersed and recur No opportunity to master one before confronted with another

# Summary: Continual Learning

• Regularization, Distillation, Architecture Expansion/Isolation



- Regularization, Distillation, Architecture Expansion/Isolation
- Frozen representation: prompt learning



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- Exploration of multimodal continual learning from embodied environments



# Few-Shot Learning and Meta-Learning



## Few-Shot Learning (FSL)

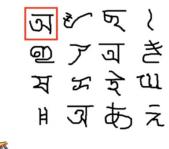
• Humans can quickly learn new concepts with a few examples.

'goldfish'

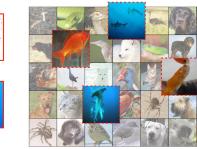
"shark"

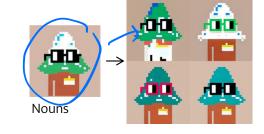
- Learning in embodied agents also needs to be adaptive and swift.
- Examples: Recognize new objects, perform new skills, map new areas, etc.





[Lake et al. 2011]





[Ren et al. 2018]

[Lu et al. 2024]



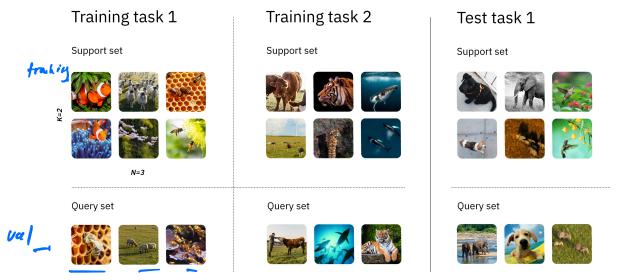
## FSL: General Setup

• Quickly learn a task (learning episode) with very few number of training examples and get evaluated on a set of test examples.



# FSL: General Setup

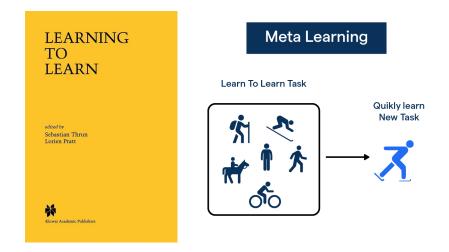
- Quickly learn a task (learning episode) with very few number of training examples and get evaluated on a set of test examples.
- During training, going through many episodes of the same structure.





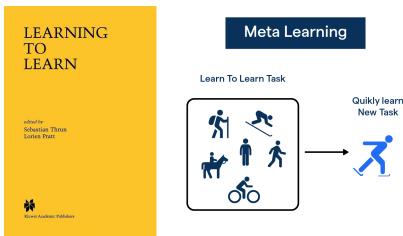
https://www.ibm.com/think/topics/few-shot-learning

• Conceptually, we'd like to generalize new learning experiences.





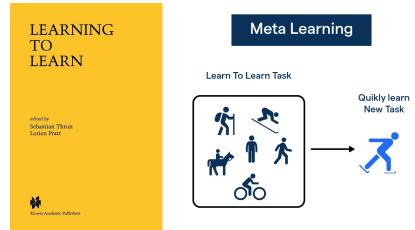
- Conceptually, we'd like to generalize new learning experiences.
- 1 learning experience = 1 training example





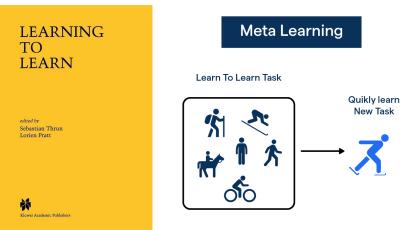


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- Related to multi-task learning



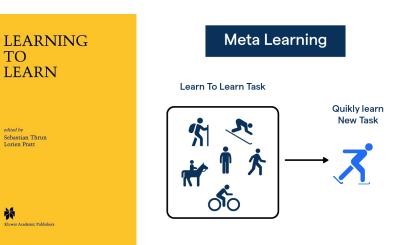


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- What can be meta-learned?
  - Optimizer
  - Initialization
  - Architecture
  - Representations
  - Abstraction of tasks





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- What can be meta-learned?
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  - Representations
  - Abstraction of tasks
- Discover learning algorithms that support FSL.





#### Meta-Optimization (Bi-level Optimization)

• One can formulate meta-learning as a meta-optimization problem.

 $\min_{\lambda} \mathbb{E} \min_{D \sim \mathcal{D}} \mathbb{E} \mathcal{L}(x; \theta, \lambda).$  hyper parameter.



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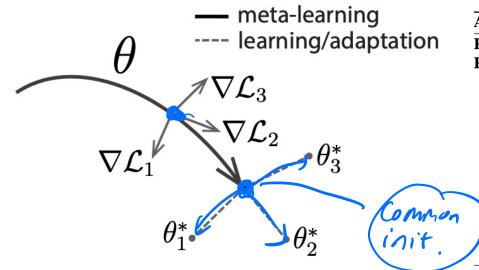
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- Need to optimize through the inner optimization.
  - BPTT
  - Fixed point (implicit differentiation)
  - Zeroth order optimization
- Short-horizon bias: Optimal actions in the next few steps may not be optimal in the long run.
  - Example: Lowering learning rate will always result in short-term gains.



## MAML (Truncated Optimization)

- For few-shot learning, short horizon is actually needed.
- Unroll the gradient graph for a few iterations.
- MAML (Model-agnostic meta-learning)



Algorithm 1 Model-Agnostic Meta-Learning

- **Require:**  $p(\mathcal{T})$ : distribution over tasks
- **Require:**  $\alpha$ ,  $\beta$ : step size hyperparameters
- 1: randomly initialize  $\theta$
- 2: while not done do
- 3: Sample batch of tasks  $\mathcal{T}_i \sim p(\mathcal{T})$
- 4: for all  $\mathcal{T}_i$  do
- 5: Evaluate  $\nabla_{\theta} \mathcal{L}_{\mathcal{T}_i}(f_{\theta})$  with respect to K examples
- 6: Compute adapted parameters with gradient descent:  $\theta'_i = \theta - \alpha \nabla_{\theta} \mathcal{L}_{\mathcal{T}_i}(f_{\theta})$

end for

Update 
$$\theta \leftarrow \theta - \beta \nabla_{\theta} \sum_{\mathcal{T}_i \sim p(\mathcal{T})} \mathcal{L}_{\mathcal{T}_i}(f_{\theta'_i})$$
  
nd while



Finn et al. Model-Agnostic Meta-Learning for Fast Adaptation of Deep Networks. ICML 2017.

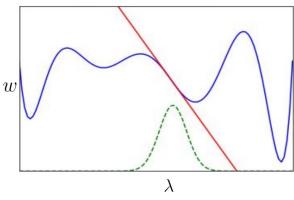
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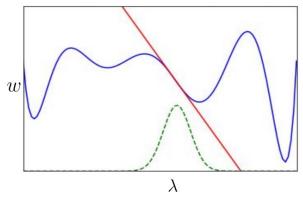


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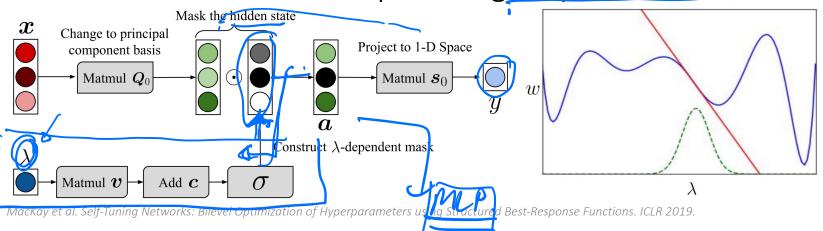




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• Prototypical Network: Few-shot Classification



- Prototypical Network: Few-shot Classification
- Prototype = Avg. representation of a class

$$\mathbf{p}_k = \frac{1}{|S_k|} \sum_{(\mathbf{x}, y) \in S_k} f_\phi(\mathbf{x}_i).$$

$$p(y = k \mid \mathbf{x}) = \operatorname{softmax}(-d(f_{\phi}(\mathbf{x}), \mathbf{p}_k)).$$

Snell et al. Prototypical Networks for Few-shot Learning. NIPS 2017. Allen et al. Infinite Mixture Prototypes for Few-Shot Learning. ICML 2019.



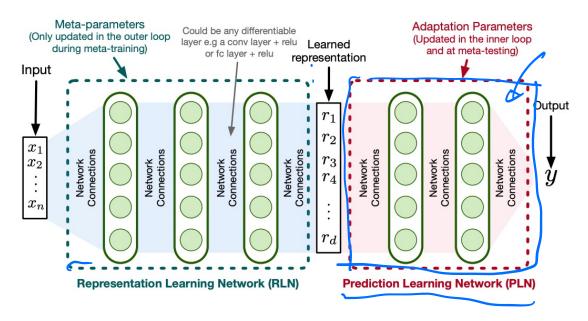
- Prototypical Network: Few-shot Classification
- Prototype = Avg. representation of a class  $\mathbf{p}_k = \frac{\mathbf{I}}{|S_k|} \sum_{(\mathbf{x}, y) \in S_k} f_{\phi}(\mathbf{x}_i).$
- 1 example = exemplar-based. Can be in between.

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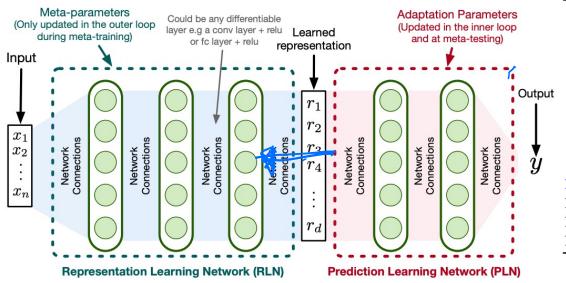


#### • Representation vs. Memory Layers





- Representation vs. Memory Layers
- Learning to continually learn

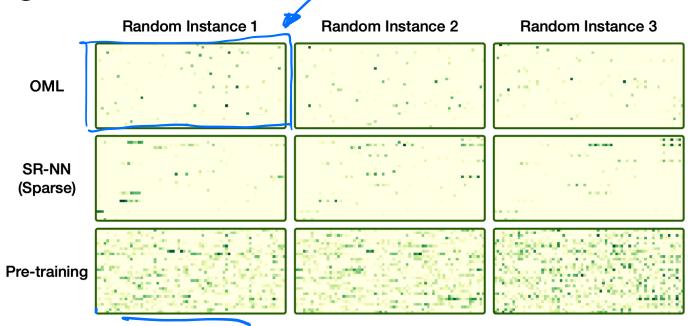


Algorithm 2: Meta-Training : OML

**Require:**  $p(\mathcal{T})$ : distribution over CLP problems **Require:**  $\alpha$ ,  $\beta$ : step size hyperparameters 1: randomly initialize  $\theta$ while not done do 2: randomly initialize W3: Sample CLP problem  $\mathcal{T}_i \sim p(\mathcal{T})$ 4: Sample  $S_{train}$  from  $p(S_k | T_i)$ 5: 6:  $W_0 = W$ 7: for j = 1, 2, ..., k do 8:  $(X_j, Y_j) = \mathcal{S}_{train}[j]$  $W_{i} = W_{i-1} - \alpha \nabla_{W_{i-1}} \ell_{i}(f_{\theta, W_{i-1}}(X_{i}), Y_{i})$ 9: 10: end for Sample  $S_{test}$  from  $p(S_k | T_i)$ 11: Update  $\theta \leftarrow \theta - \beta \nabla_{\theta} \ell_i(f_{\theta, W_k}(S_{test}[:, 0]), S_{test}[:, 1])$ 12: 13: end while

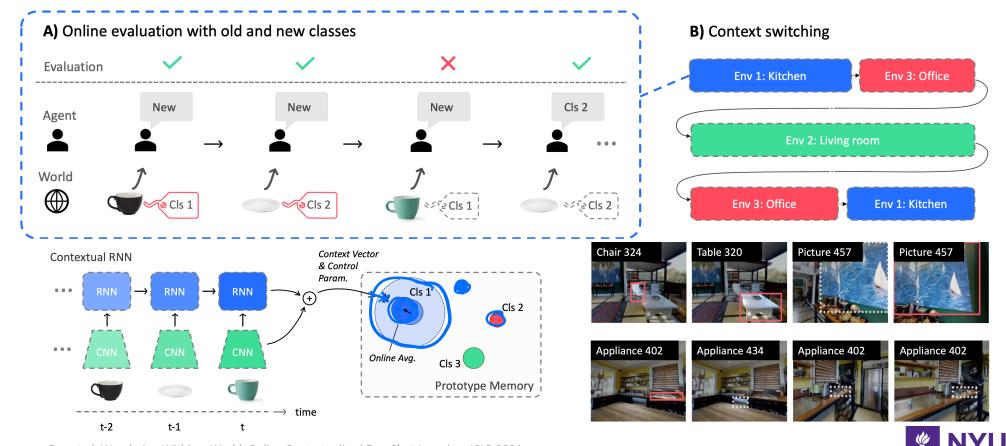


• Meta-learning leads to sparse representation suitable for continual learning.









Ren et al. Wandering Within a World: Online Contextualized Few-Shot Learning. ICLR 2021.

• Compared to OML: Using prototype memory vs. generic MLP.



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- Both learning representations through online learning episodes.

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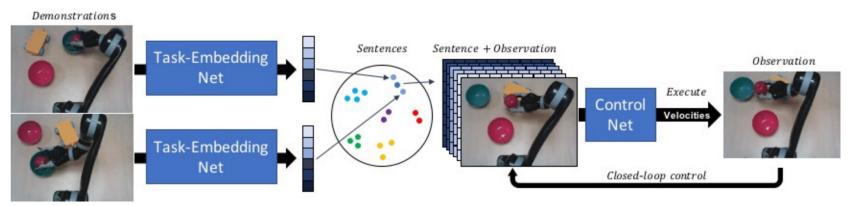
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#### Few-Shot Imitation Learning

• The idea of prototype learning can also be applied to skill learning.

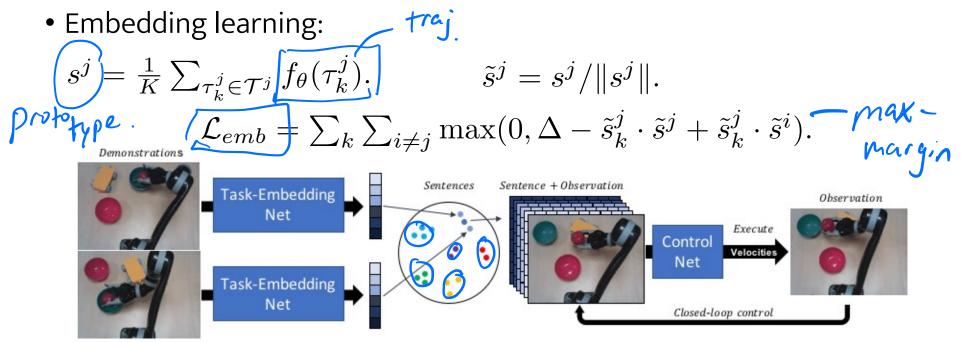


Finn et al. One-Shot Visual Imitation Learning via Meta-Learning. CoRL 2017. James et al. Task-Embedded Control Networks for Few-Shot Imitation Learning. CoRL 2018.



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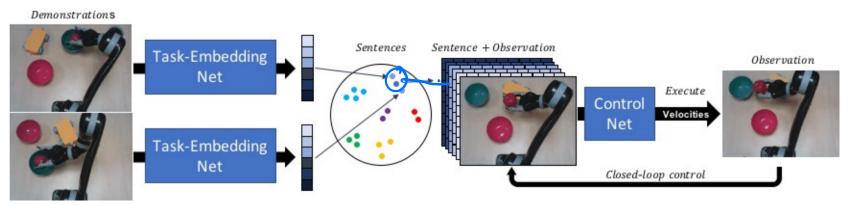


#### Few-Shot Imitation Learning

D

• Control learning:

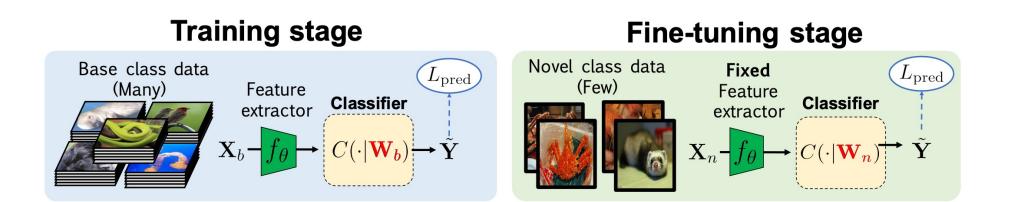
$$\mathcal{L}_{ctr} = \sum_{j} \sum_{(o,a) \in \tau^{j}} \| \pi(o, s^{j}) - a \|_{2}^{2}$$





### Leveraging Pretrained Representations

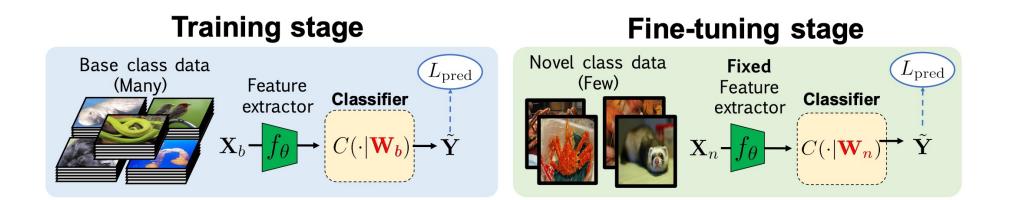
• Need a strong pretrained network.





### Leveraging Pretrained Representations

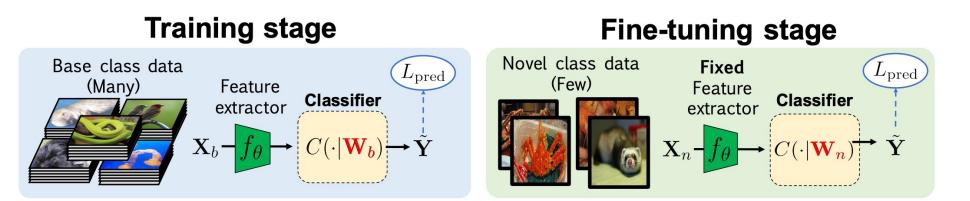
- Need a strong pretrained network.
- Works well for few-shot classification.





### Leveraging Pretrained Representations

- Need a strong pretrained network.
- Works well for few-shot classification.
- Once again proves that representation is crucial.



#### 🌾 NYU

#### In-Context Learning (ICL)

• Traditionally, learning through parameters  $\theta$ .



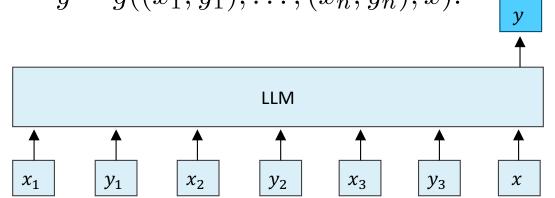
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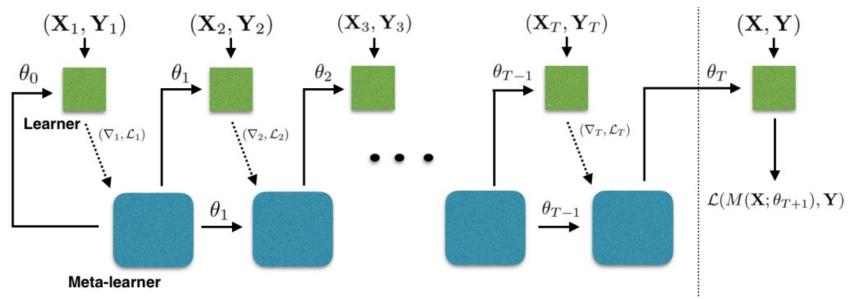
- Traditionally, learning through parameters  $\theta$ .
- ICL does not optimize any parameters, just put the training data in the context.
- Inner optimization loop done in a sequence model (RNN, Transformer, etc.)  $y = g((x_1, y_1), \dots, (x_n, y_n), x).$





### Meta-Learning LSTM

- An earlier sequential meta-learning paradigm before ICL.
- Using hidden states as "parameters"

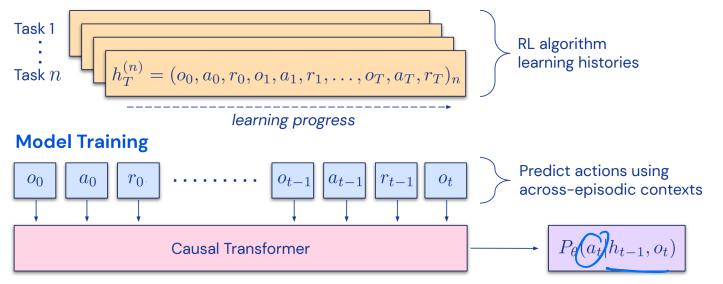




#### In-Context RL

• Use sequences of Obervation  $(o_t)$ , Action  $(a_t)$  and Reward  $(r_t)$  generated by standard RL algorithms.

#### **Data Generation**





## Test-Time Tuning/Adaptation

- Context Retrieval, e.g. nearest neighbors
- Finetuning on examples
  - Full finetuning
  - Low-rank adaptation
  - Prompt tuning
- Self-supervision objectives



- A modularized but differentiable end-to-end architecture
  - Perception
  - Prediction
  - Planning
  - Mapping
  - Memory



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  - Reconstruction
    Future prediction 
    Reinforcement learning



• Useful inductive biases



- Useful inductive biases
  - Spatial grounding



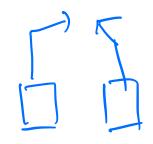
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  - Memory, replay, sparsity
  - Learning inductive biases, learning to learn



### **Topic Presentations**

#### Component 1

Continual Learning, Few-shot Week 7 (Mar 6) Learning (1 hr) Week 8 (Mar 13) Guest Lecture -, Prof. Wei-Chiu Ma (1 hr) Week 9 (Mar 20) SSL and Object Discovery Anurup Naskar, Dahye Kim, Sal Yeung, Surbhi (1.5 hr) World Model 2 Week 11 (Apr 3) Pratyaksh Prabhav Rao, Sergey Sedov, Rooholla Khorrambakht Week 12 (Apr 10) **Continual Learning** Akshay Raman, Amey Joshi, **Zifan Zhao** Week 13 (Apr 17) Guest Lecture – Dr. Andrei Barsan (1hr)

#### Component 2

**Deep Learning for Structured Prediction** Tanishq Sardana, Qing Mu, Owais Shuja

**3D Vision and Mapping** Sihang Li, Kanishkha Jaisankar, Denis Mbey Akola, Zijin Hu

World Model 1 Sidhartha Reddy Potu, Andrew Deur

#### **End-to-End Planning** Raman Kumar Jha, Jovita Gandhi, Sushma Mareddy, Mrunal Sarvaiya

**Few-Shot Learning** Ellen Su, Xu Zhang, Swarali Borde

LLM Agents Solim LeGris, Ravan Budda, Dan Zhao, Sunidhi Tandel



#### **Project Presentations**

Week 14 (Apr 24)	Project Presentations (7 teams)
Week 15 (May 1)	Project Presentations (7 teams)

- Apr 10: Sign up for a presentation slot. Week 14 Presenters get 2% bonus. First come first serve.
- Project topics and proposals to be shared in the class.



# Today

- Tanishq Sardana: Segment Anything
- Qing Mu: DETR: End-to-End Object Detection
- Owais Saad Shuja: Latent Diffusion Models
- Discussion

